

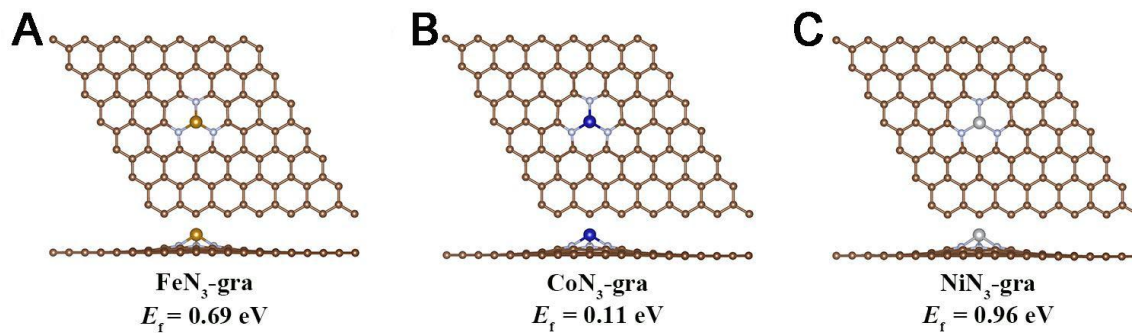
*Supplementary Materials*

**High hydrogen evolution activities of dual-metal atoms incorporated N-doped graphenes achieved by coordination regulation**

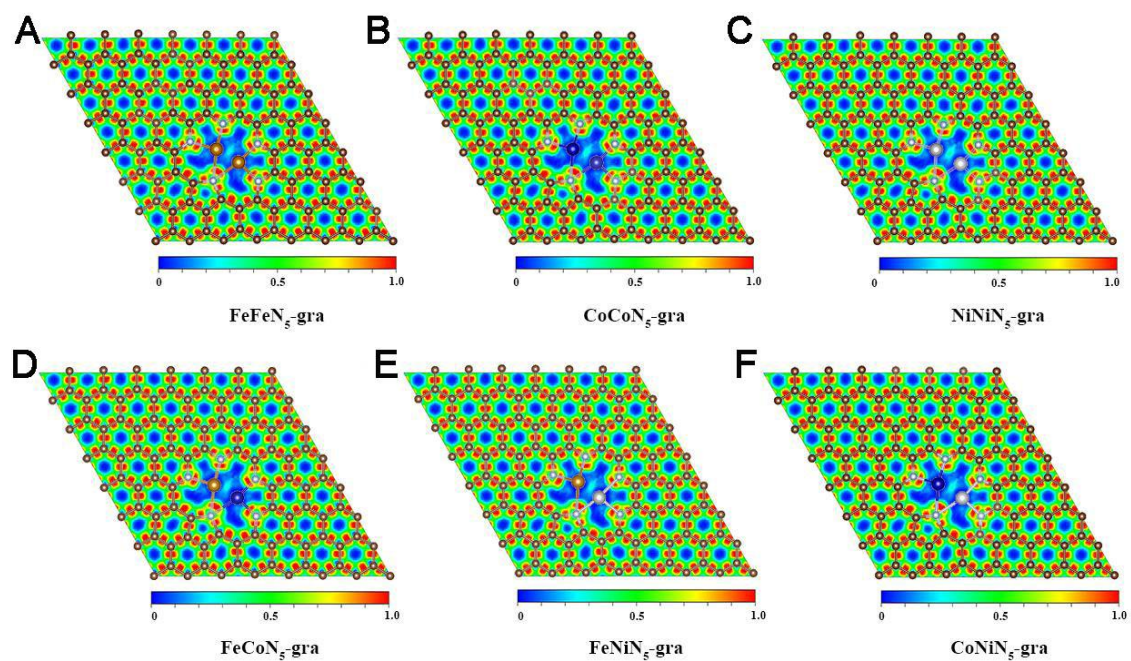
Cunjin Zhang, Shuaibo Qin, Hui Gao, Peng Jin\*

School of Materials Science and Engineering, Hebei University of Technology, Tianjin  
300130, China. *E-mail*: pengjin@hebut.edu.cn

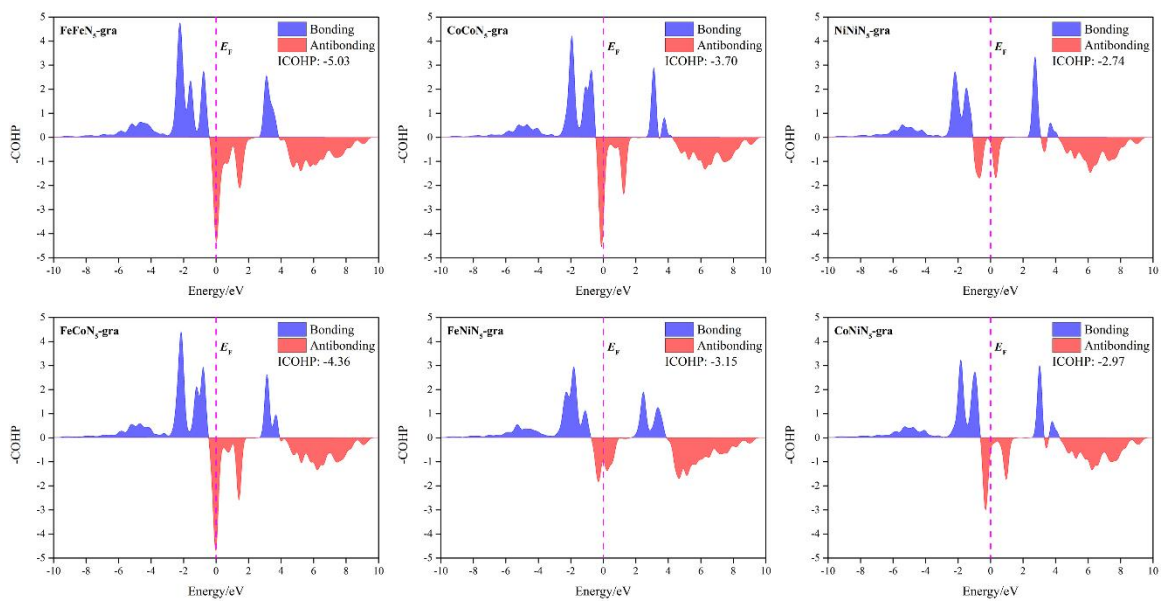
## Supplementary Figures



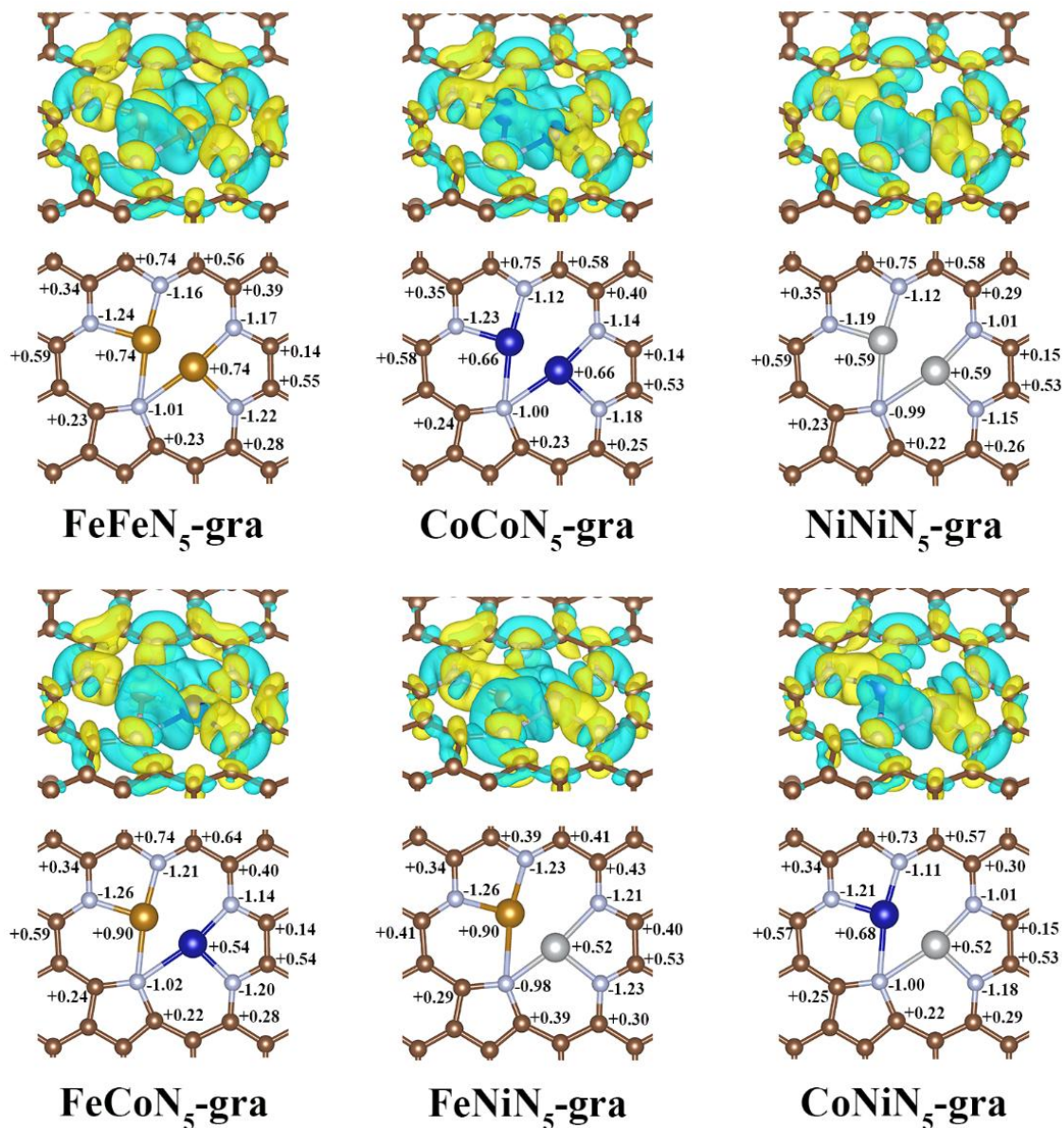
**Supplementary Figure 1.** Optimized structures (top and side views) and formation energies ( $E_f$ ) of the three single-atom catalysts. (A)-(C) MN<sub>3</sub>-gra (M = Fe, Co, Ni). C: brown; N: light blue; Fe: golden; Co: dark blue; Ni: silvery.



**Supplementary Figure 2.** Electron localization functions (ELFs) for the N-doped graphene planes of all the catalysts shown in Figure 3 of main text.



**Supplementary Figure 3.** Crystal orbital Hamilton population (COHP) and integrated-COHP (ICOHP) between the two adjacent metal atoms of MMN<sub>5</sub>-gra and M1M2N<sub>5</sub>-gra.

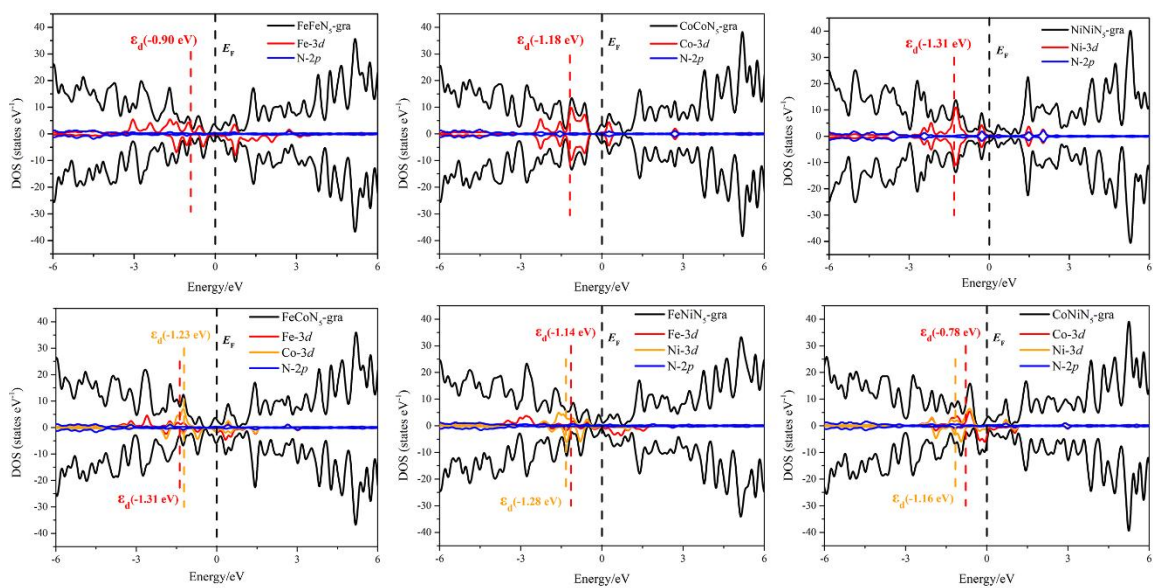


**Supplementary Figure 4.** Charge density difference (upper) and Bader charges (down) of MMN<sub>5</sub>-gra/M1M2N<sub>5</sub>-gra catalysts. The yellow and cyan colors denote the electron accumulation and depletion, respectively. The charge density difference was calculated as follows:

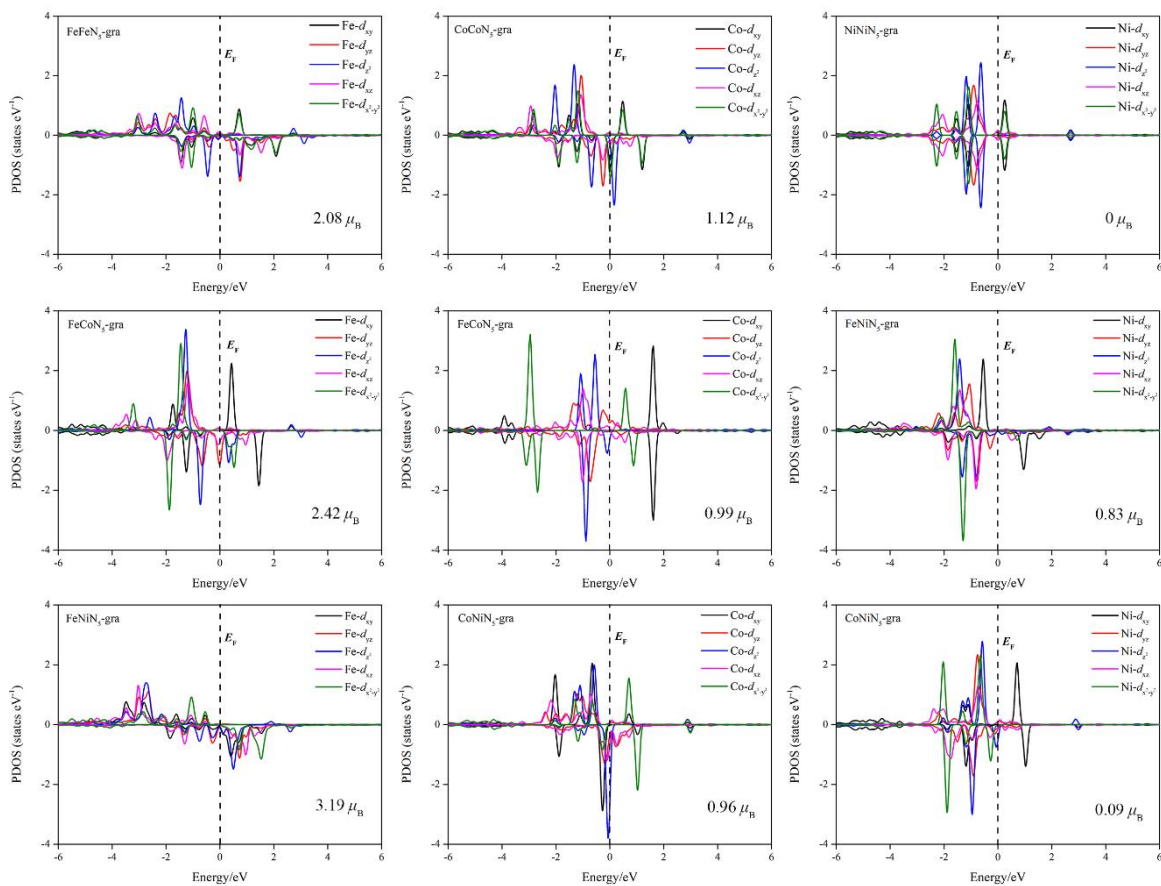
$$\Delta\rho(r) = \rho(r)_{\text{MMN}_5\text{-gra}} - \rho(r)_{\text{MM}} - \rho(r)_{\text{N}_5\text{-gra}}$$

$$\Delta\rho(r) = \rho(r)_{\text{M1M2N}_5\text{-gra}} - \rho(r)_{\text{M1M2}} - \rho(r)_{\text{N}_5\text{-gra}}$$

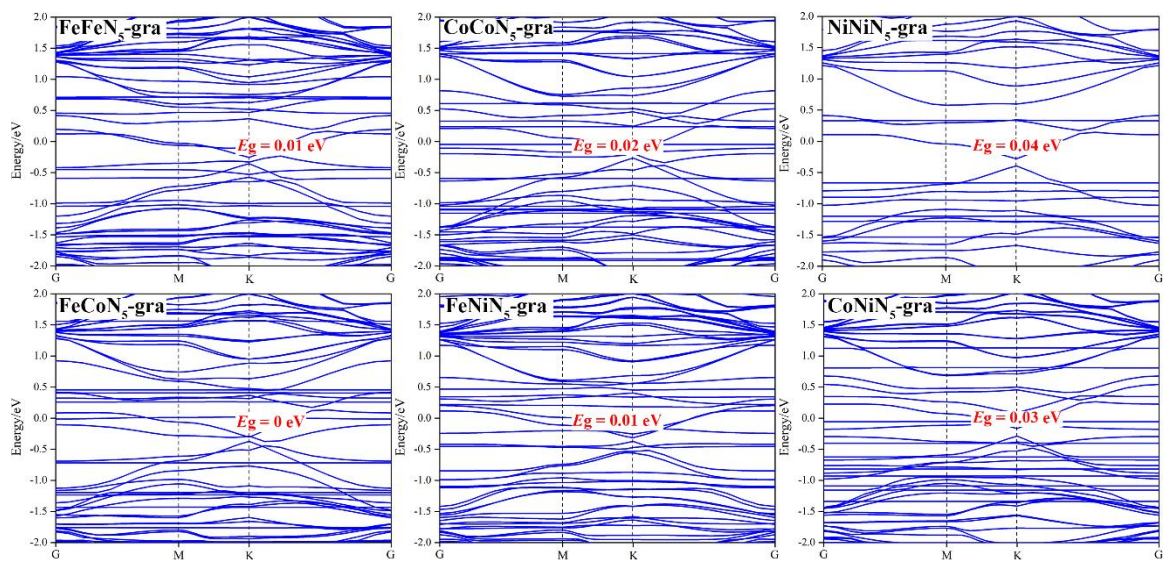
where  $\rho(r)_{\text{MMN}_5\text{-gra}}$  and  $\rho(r)_{\text{M1M2N}_5\text{-gra}}$  are the charge density of the catalysts,  $\rho(r)_{\text{N}_5\text{-gra}}$  is the charge density of the catalysts without metals, and  $\rho(r)_{\text{MM}}$  and  $\rho(r)_{\text{M1M2}}$  are the charge density of the metal atoms.



**Supplementary Figure 5.** Total DOSs and projected M-3d and N-2p states of all MMN<sub>5</sub>-gra/M1M2N<sub>5</sub>-gra catalysts with the metal d-band centers ( $\epsilon_d$ ) calculated from both spin up and spin down states. Fermi levels are set at 0 eV.

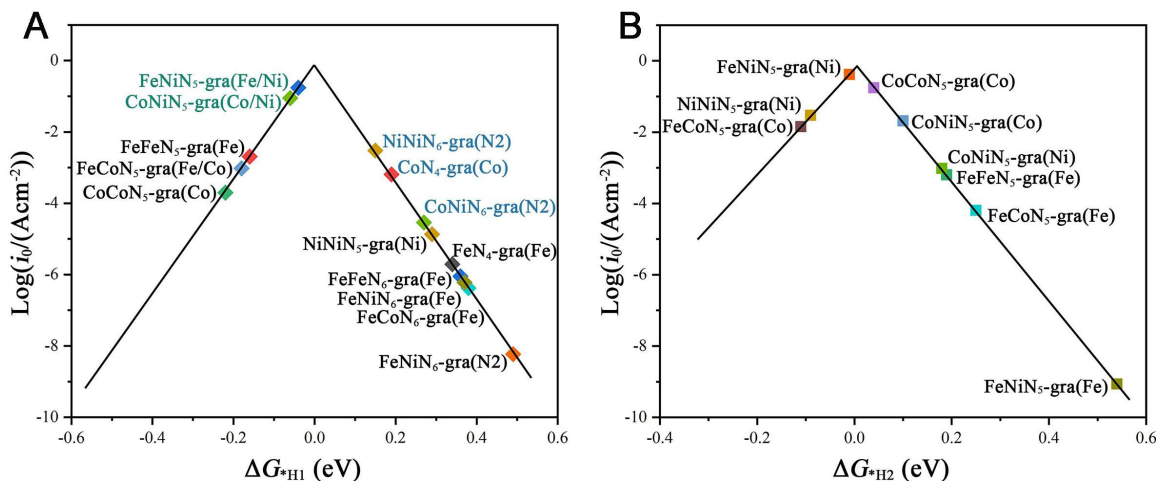


**Supplementary Figure 6.** Projected DOSs of M-3d states (both spin up and spin down) and metal spin moment of all MMN<sub>5</sub>-gra/M1M2N<sub>5</sub>-gra catalysts. Fermi levels are set at 0 eV.



**Supplementary Figure 7.** Electronic band structures of MMN<sub>5</sub>-gra/M<sub>1</sub>M<sub>2</sub>N<sub>5</sub>-gra catalysts.





**Supplementary Figure 8.** Volcanic curve of the exchange current ( $i_0$ ) as a function of the  $\Delta G^*_{\text{H}}$  values for the adsorption of (A) first and (B) second hydrogen atoms. In (B) only those with high activity in both (A) and (B) are considered to be promising catalysts following the H<sub>2</sub>MH intermediate mechanism.

The theoretical exchange current was calculated by using the following equations as done in the recent literature<sup>[1]</sup>:

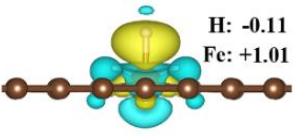
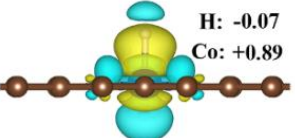
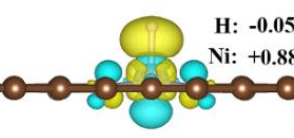
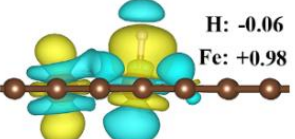
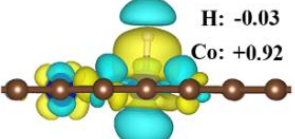
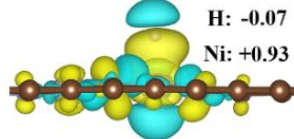
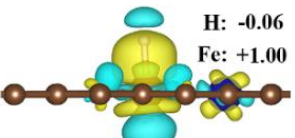
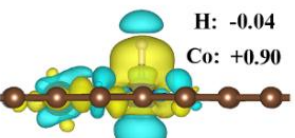
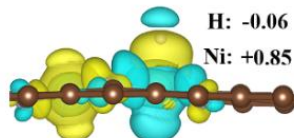
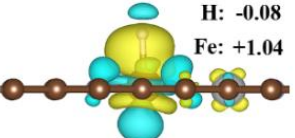
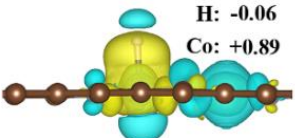
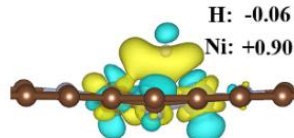
If  $\Delta G^*_{\text{H}} \leq 0$

$$i_0 = -ek_0/(1+\exp(-\Delta G^*_{\text{H}}/k_{\text{B}}T)) \quad (1)$$

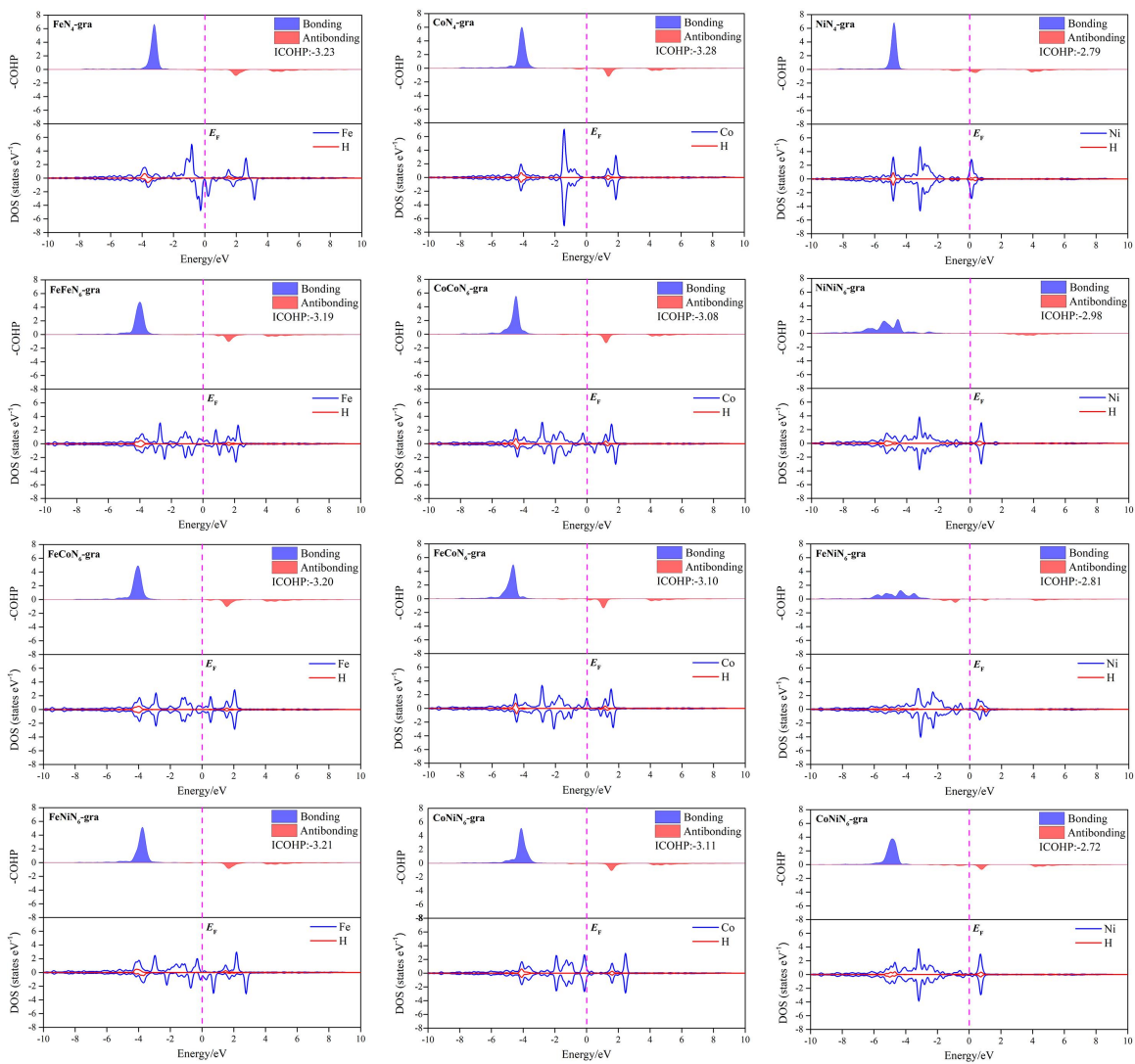
If  $\Delta G^*_{\text{H}} > 0$

$$i_0 = -ek_0/(1+\exp(\Delta G^*_{\text{H}}/k_{\text{B}}T)) \quad (2)$$

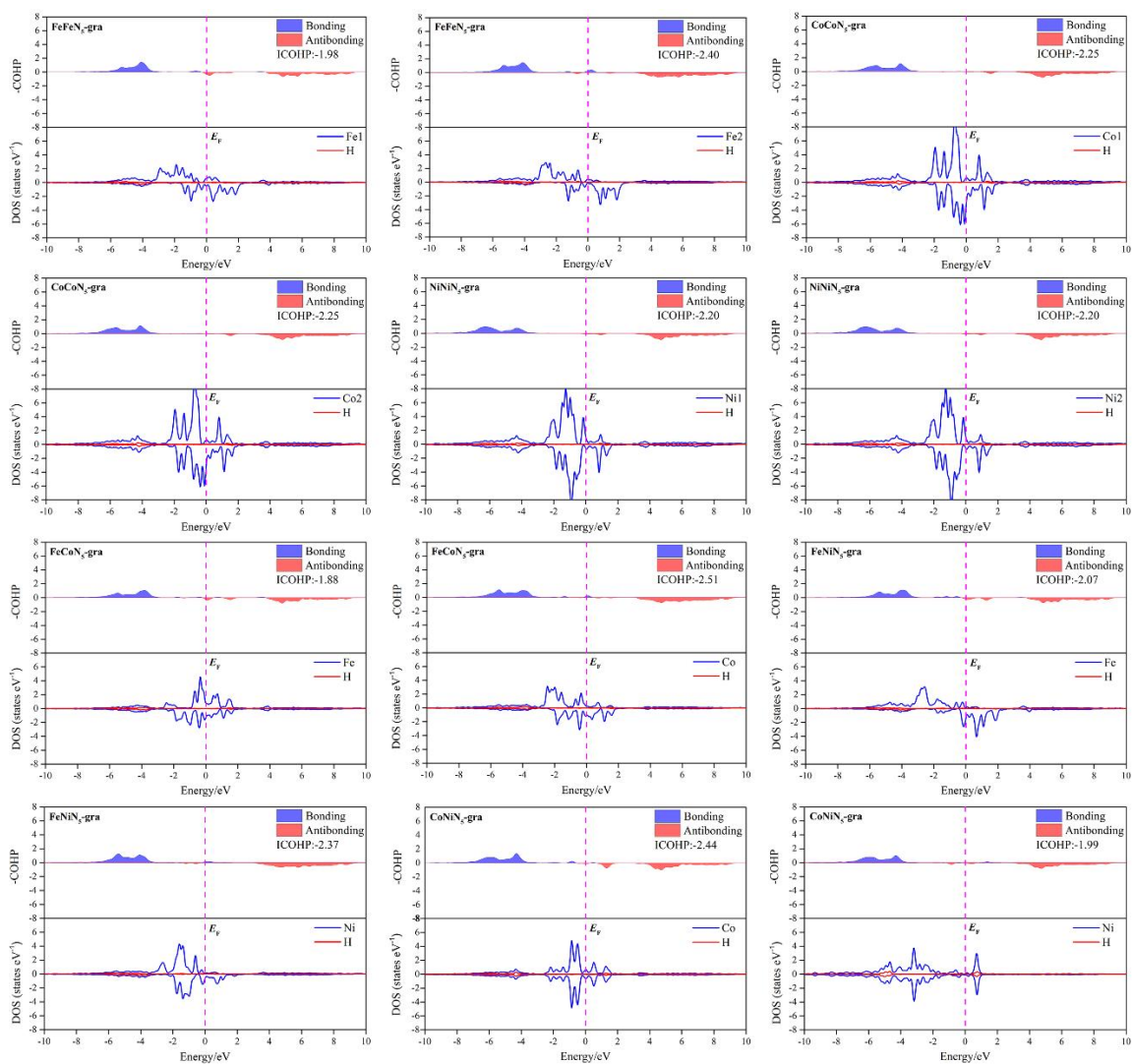
where rate constant ( $k_0$ ) is set to 1,  $k_{\text{B}}$  is the Boltzmann constant ( $1.38064 \times 10^{-23}$  J/K) and  $T$  is temperature (298.15 K).

<p><b>FeN<sub>4</sub>-gra</b></p>  <p>H: -0.11 Fe: +1.01</p>	<p><b>CoN<sub>4</sub>-gra</b></p>  <p>H: -0.07 Co: +0.89</p>	<p><b>NiN<sub>4</sub>-gra</b></p>  <p>H: -0.05 Ni: +0.88</p>
<p><b>FeFeN<sub>6</sub>-gra</b></p>  <p>H: -0.06 Fe: +0.98</p>	<p><b>CoCoN<sub>6</sub>-gra</b></p>  <p>H: -0.03 Co: +0.92</p>	<p><b>NiNiN<sub>6</sub>-gra</b></p>  <p>H: -0.07 Ni: +0.93</p>
<p><b>FeCoN<sub>6</sub>-gra (Fe site)</b></p>  <p>H: -0.06 Fe: +1.00</p>	<p><b>FeCoN<sub>6</sub>-gra (Co site)</b></p>  <p>H: -0.04 Co: +0.90</p>	<p><b>FeNiN<sub>6</sub>-gra (Ni site)</b></p>  <p>H: -0.06 Ni: +0.85</p>
<p><b>FeNiN<sub>6</sub>-gra (Fe site)</b></p>  <p>H: -0.08 Fe: +1.04</p>	<p><b>CoNiN<sub>6</sub>-gra (Co site)</b></p>  <p>H: -0.06 Co: +0.89</p>	<p><b>CoNiN<sub>6</sub>-gra (Ni site)</b></p>  <p>H: -0.06 Ni: +0.90</p>

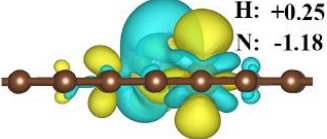
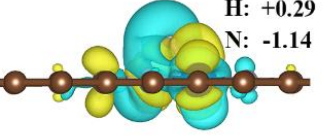
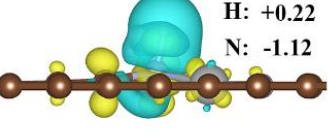
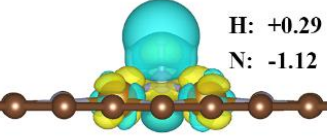
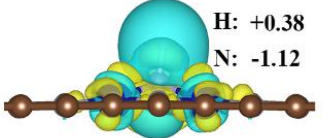
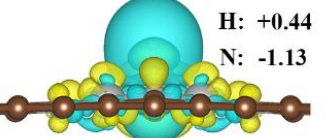
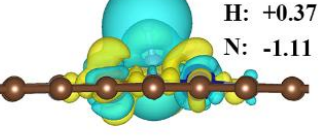
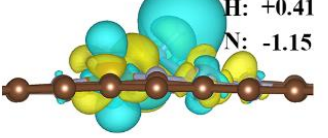
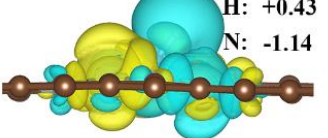
**Supplementary Figure 9.** The charge density difference and Bader charge when the hydrogen evolution reaction occurs on the metal site for MN<sub>4</sub>-gra/MMN<sub>6</sub>-gra/M1M2N<sub>6</sub>-gra.



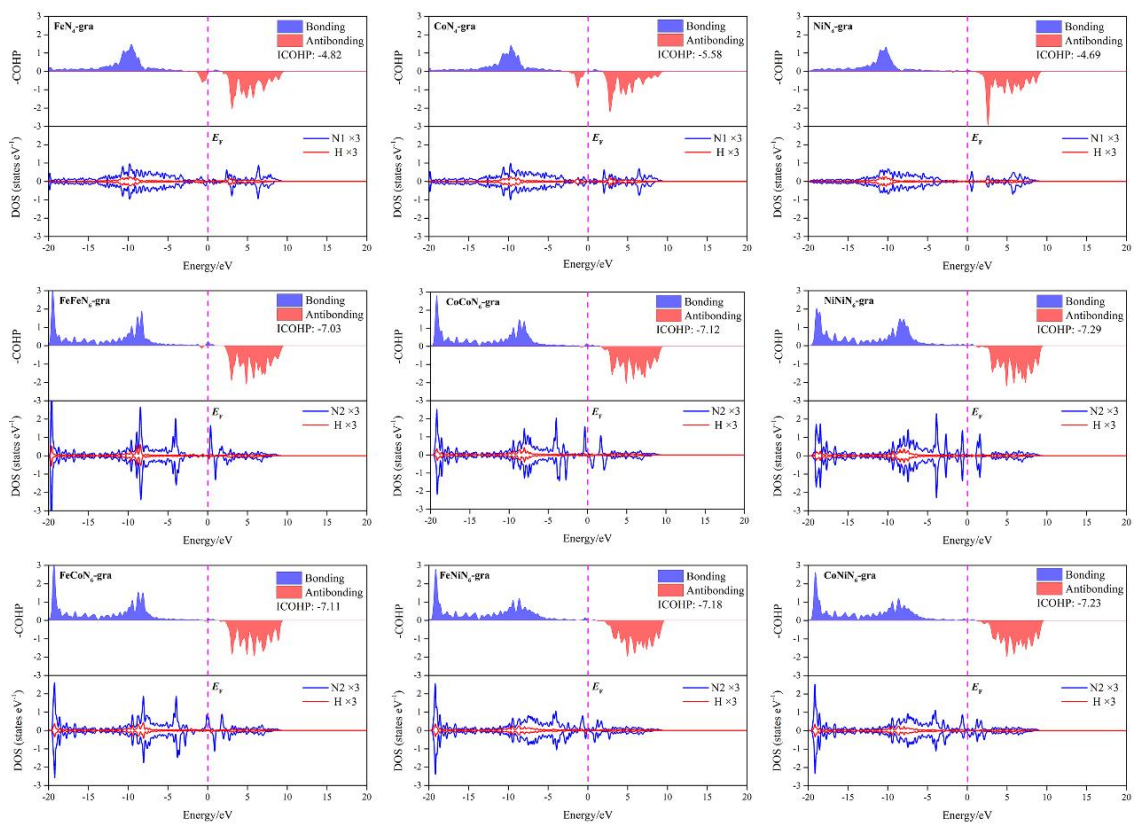
**Supplementary Figure 10.** Crystal orbital Hamiltonian population (COHP) between M-H in \*H for MN<sub>4</sub>-gra/MMN<sub>6</sub>-gra/M1M2N<sub>6</sub>-gra.



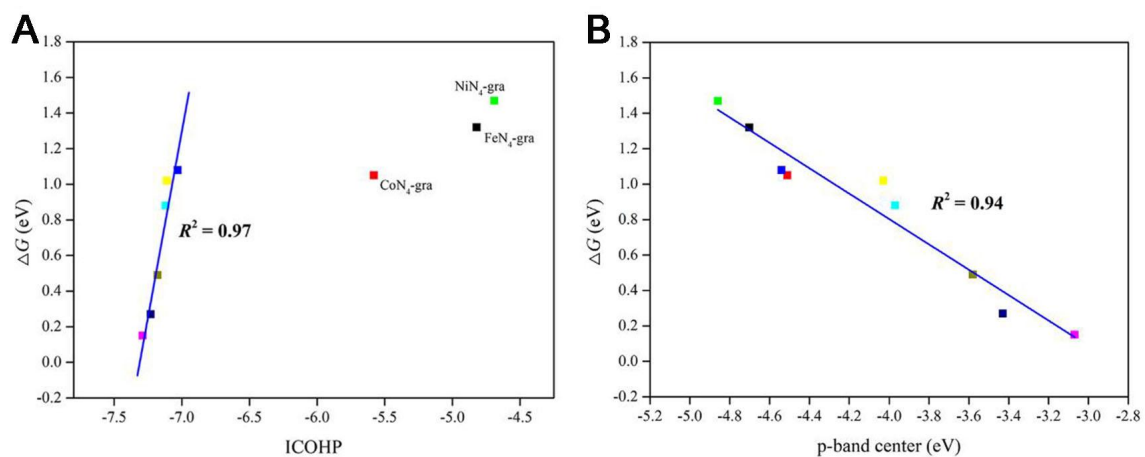
**Supplementary Figure 11.** Crystal orbital Hamiltonian population (COHP) between M-H in \*H for  $MMN_5$ -gra/ $M1M2N_5$ -gra.

<p>FeN<sub>4</sub>-gra (N1 site)</p>  <p>H: +0.25 N: -1.18</p>	<p>CoN<sub>4</sub>-gra (N1 site)</p>  <p>H: +0.29 N: -1.14</p>	<p>NiN<sub>4</sub>-gra (N1 site)</p>  <p>H: +0.22 N: -1.12</p>
<p>FeFeN<sub>6</sub>-gra (N2 site)</p>  <p>H: +0.29 N: -1.12</p>	<p>CoCoN<sub>6</sub>-gra (N2 site)</p>  <p>H: +0.38 N: -1.12</p>	<p>NiNiN<sub>6</sub>-gra (N2 site)</p>  <p>H: +0.44 N: -1.13</p>
<p>FeCoN<sub>6</sub>-gra (N2 site)</p>  <p>H: +0.37 N: -1.11</p>	<p>FeNiN<sub>6</sub>-gra (N2 site)</p>  <p>H: +0.41 N: -1.15</p>	<p>CoNiN<sub>6</sub>-gra (N2 site)</p>  <p>H: +0.43 N: -1.14</p>

**Supplementary Figure 12.** The charge density difference and Bader charge when the hydrogen evolution reaction occurs on the N site for MN<sub>4</sub>-gra/MMN<sub>6</sub>-gra/M1M2N<sub>6</sub>-gra.



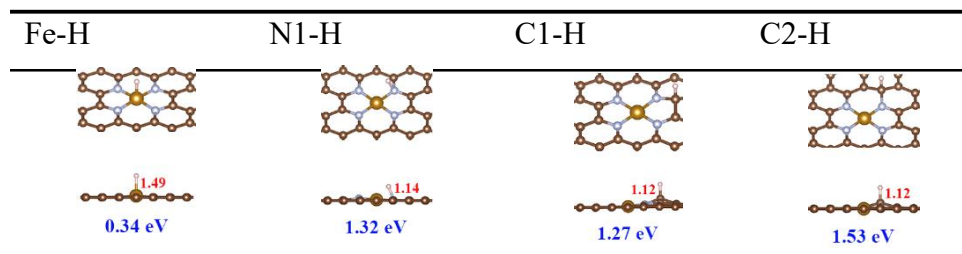
**Supplementary Figure 13.** Crystal orbital Hamiltonian population (COHP) between N-H in \*H for MN<sub>4</sub>-gra/MMN<sub>6</sub>-gra/M1M2N<sub>6</sub>-gra.



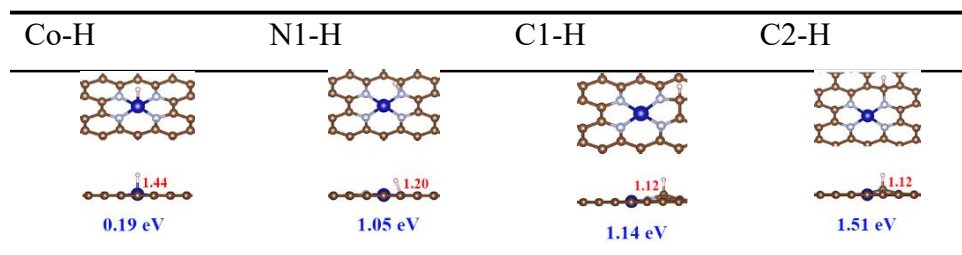
**Supplementary Figure 14.** (A) Linear relationship between N-H crystal orbital Hamiltonian population integral (ICOHP) and free energy of H adsorption for MN<sub>4</sub>-gra/MMN<sub>6</sub>-gra/M1M2N<sub>6</sub>-gra; (B) Linear relationship between the p-band centers of the nitrogen atom and free energy of H adsorption.

## Supplementary Tables

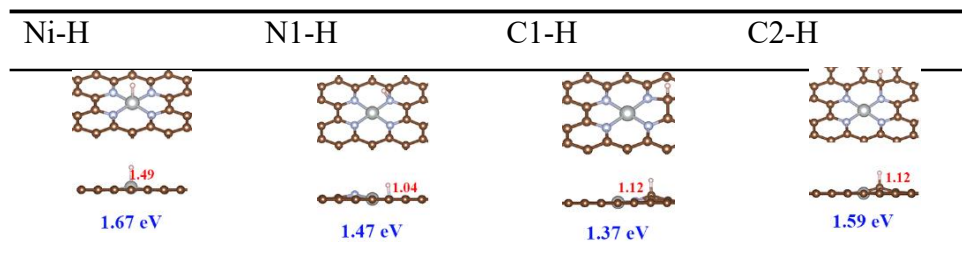
**Supplementary Table 1.** Potential \*H adsorption structures (distance unit: Å) and adsorption free energies on FeN<sub>4</sub>-gra.



**Supplementary Table 2.** Potential \*H adsorption structures (distance unit: Å) and adsorption free energies on CoN<sub>4</sub>-gra.

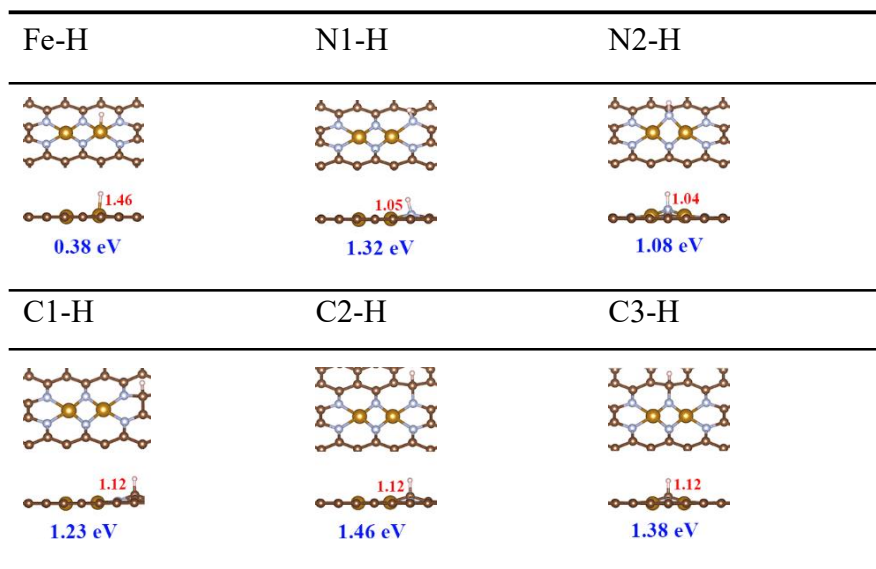


**Supplementary Table 3.** Potential \*H adsorption structures (distance unit: Å) and adsorption free energies on NiN<sub>4</sub>-gra.

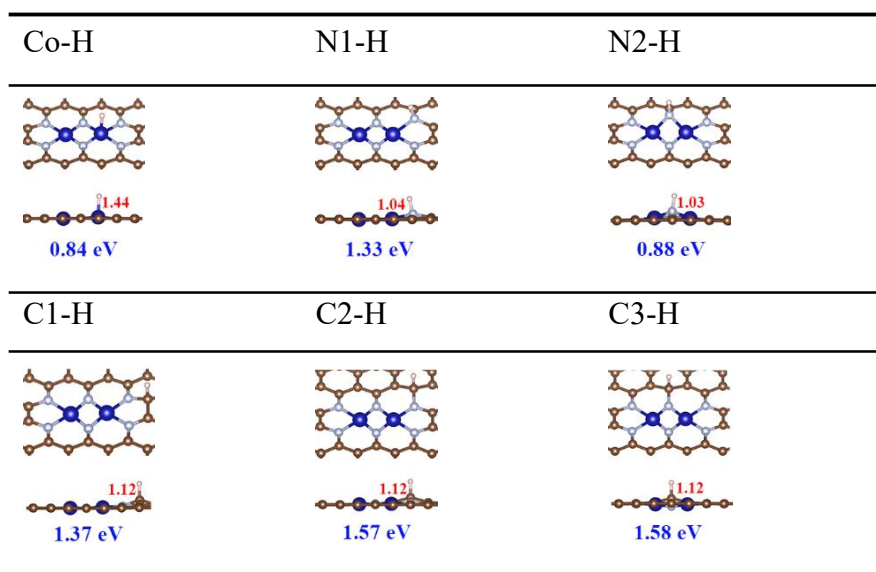




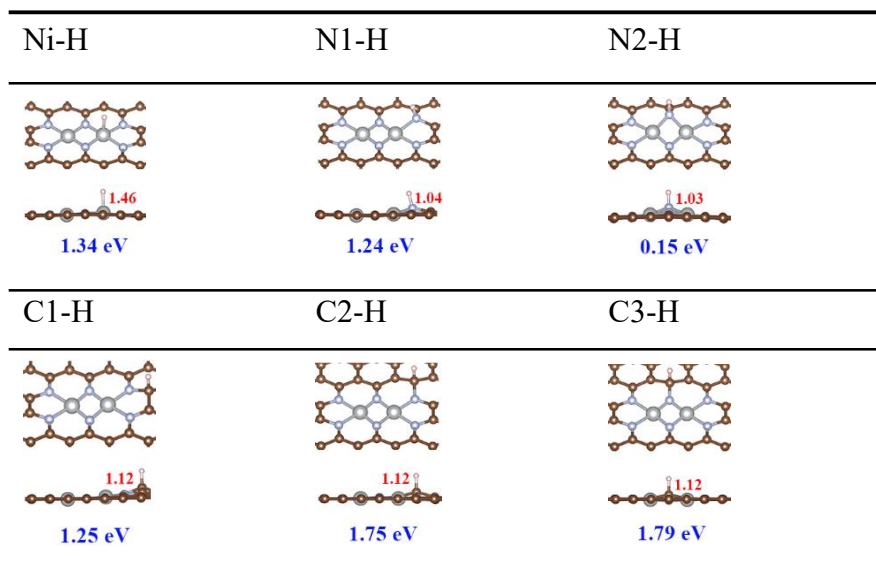
**Supplementary Table 4.** Potential \*H adsorption structures (distance unit: Å) and adsorption free energies on FeFeN<sub>6</sub>-gra.



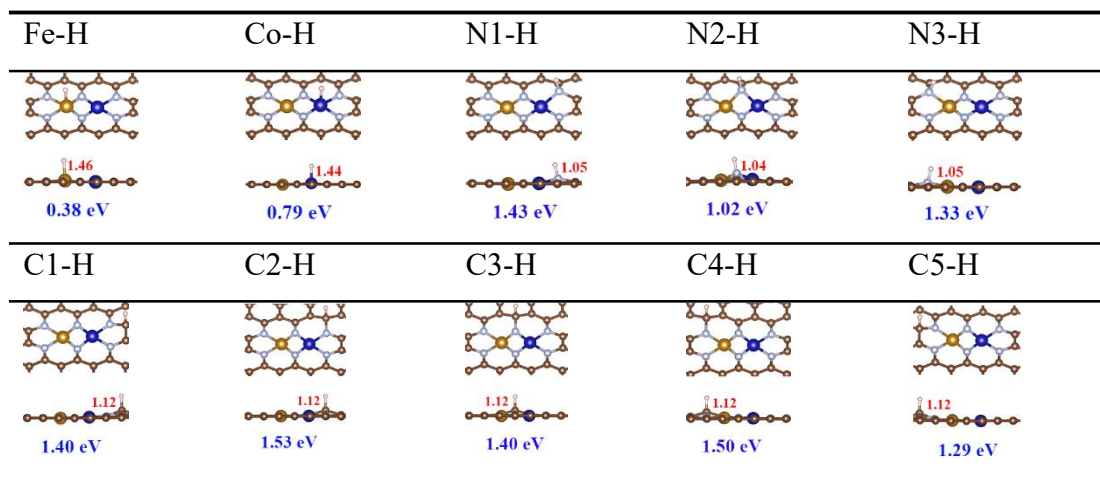
**Supplementary Table 5.** Potential \*H adsorption structures (distance unit: Å) and adsorption free energies on CoCoN<sub>6</sub>-gra.



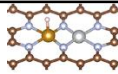
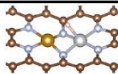
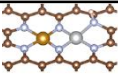
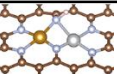
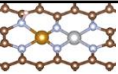





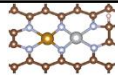
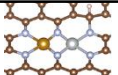
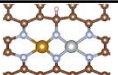
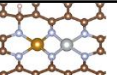
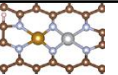





**Supplementary Table 6.** Potential \*H adsorption structures (distance unit: Å) and adsorption free energies on NiNiN<sub>6</sub>-gra.



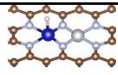
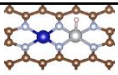
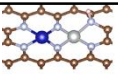
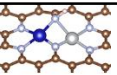
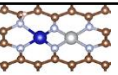





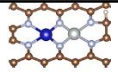
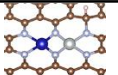
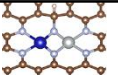
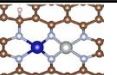
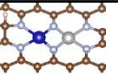





**Supplementary Table 7.** Potential \*H adsorption structures (distance unit: Å) and adsorption free energies on FeCoN<sub>6</sub>-gra.



**Supplementary Table 8.** Potential \*H adsorption structures (distance unit: Å) and adsorption free energies on FeNiN<sub>6</sub>-gra.

Fe-H	Ni-H	N1-H	N2-H	N3-H
				
 0.37 eV	 1.66 eV	 1.24 eV	 0.49 eV	 1.51 eV
C1-H	C2-H	C3-H	C4-H	C5-H
				
 1.38 eV	 1.53 eV	 1.59 eV	 1.50 eV	 1.15 eV

**Supplementary Table 9.** Potential \*H adsorption structures (distance unit: Å) and adsorption free energies on CoNiN<sub>6</sub>-gra.

Co-H	Ni-H	N1-H	N2-H	N3-H
				
 0.62 eV	 1.69 eV	 1.26 eV	 0.27 eV	 1.27 eV
C1-H	C2-H	C3-H	C4-H	C5-H
				
 1.31 eV	 1.57 eV	 1.61 eV	 1.58 eV	 1.27 eV

**Supplementary Table 10.** The d-band centers (eV) of metal sites on MN<sub>4</sub>-gra, MMN<sub>6</sub>-gra, and M1M2N<sub>6</sub>-gra catalysts.

<b>Model</b>	<b>Fe</b>	<b>Co</b>	<b>Ni</b>
FeN <sub>4</sub> -gra	-0.98	N/A	N/A
CoN <sub>4</sub> -gra	N/A	-1.08	N/A
NiN <sub>4</sub> -gra	N/A	N/A	-2.02
FeFeN <sub>6</sub> -gra	-1.26	N/A	N/A
CoCoN <sub>6</sub> -gra	N/A	-1.67	N/A
NiNiN <sub>6</sub> -gra	N/A	N/A	-1.73
FeCoN <sub>6</sub> -gra	-1.25	-1.56	N/A
FeNiN <sub>6</sub> -gra	-1.17	N/A	-2.08
CoNiN <sub>6</sub> -gra	N/A	-1.42	-2.20

**Supplementary Table 11.** Average distances ( $d_{M-N}$ , Å) vs. sum of covalent radii ( $r_M + r_N$ , Å) of the metal and N atoms, and the distances ( $d_{M-M}$ , Å) vs. sum of covalent radii ( $r_M + r_M$ , Å) of two adjacent metal atoms.

<b>Model</b>	$d_{M-N}$	$r_M + r_N$	$d_{M-M}$	$r_M + r_M$
FeFeN <sub>5</sub> -gra	2.07	2.38	1.92	3.34
CoCoN <sub>5</sub> -gra	2.05	1.97	1.97	2.52
NiNiN <sub>5</sub> -gra	2.03	1.88	2.06	2.34
FeCoN <sub>5</sub> -gra	2.05/2.05	2.38/1.97	1.93	2.93
FeNiN <sub>5</sub> -gra	2.14/2.05	2.38/1.88	2.09	2.84
CoNiN <sub>5</sub> -gra	2.03/2.03	1.97/1.88	2.05	2.43

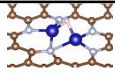
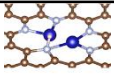
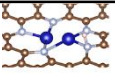
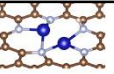
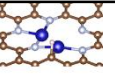
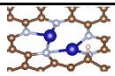
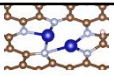
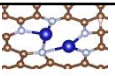
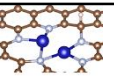
**Supplementary Table 12.** Crystal orbital overlaps between the two adjacent metal atoms of  $MMN_5$ -gra and  $M1M2N_5$ -gra. The isovalues are given in a.u.

Model	$d_{x^2-y^2}$	$d_{xy}$	$d_{z^2}$	$d_{yz}$	$d_{xz}$
FeFeN <sub>5</sub> -gra	 $4.0 \times 10^{-7}$	 $2.0 \times 10^{-7}$	 $5.0 \times 10^{-8}$	 $2.0 \times 10^{-7}$	 $3.0 \times 10^{-7}$
CoCoN <sub>5</sub> -gra	 $2.0 \times 10^{-7}$	 $2.0 \times 10^{-7}$	 $2.0 \times 10^{-7}$	 $2.0 \times 10^{-7}$	 $2.0 \times 10^{-7}$
NiNiN <sub>5</sub> -gra	 $3.0 \times 10^{-7}$	 $2.0 \times 10^{-7}$	 $5.0 \times 10^{-8}$	 $2.0 \times 10^{-7}$	 $2.0 \times 10^{-7}$
FeCoN <sub>5</sub> -gra	 $2.0 \times 10^{-7}$	 $2.0 \times 10^{-7}$	 $5.0 \times 10^{-8}$	 $5.0 \times 10^{-7}$	 $2.0 \times 10^{-7}$
FeNiN <sub>5</sub> -gra	 $2.0 \times 10^{-7}$	 $2.0 \times 10^{-7}$	 $5.0 \times 10^{-8}$	 $2.0 \times 10^{-7}$	 $1.0 \times 10^{-7}$
CoNiN <sub>5</sub> -gra	 $2.0 \times 10^{-7}$	 $2.0 \times 10^{-7}$	 $2.0 \times 10^{-7}$	 $2.0 \times 10^{-7}$	 $2.0 \times 10^{-7}$

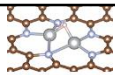
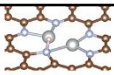
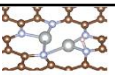
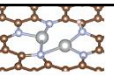
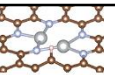
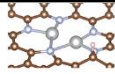
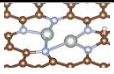
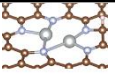
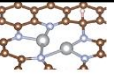
**Supplementary Table 13.** Potential \*H adsorption structures (distance unit: Å) and adsorption free energies on FeFeN<sub>5</sub>-gra.

Fe-H	N1-H	N2-H	N3-H	C1-H
 1.78, 1.65 -0.16 eV	 1.04 1.02 eV	 1.04 1.14 eV	 1.05 1.17 eV	 1.14 -1.19 eV
C2-H	C3-H	C4-H	C5-H	
 1.12 1.15 eV	 1.04 1.14 eV	 1.12 1.13 eV	 1.12 1.22 eV	

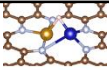
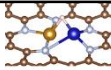
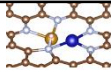
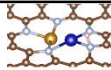
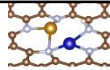
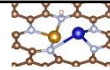
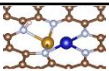
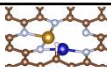
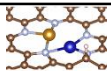
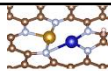
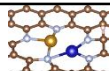
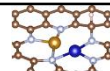
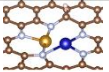
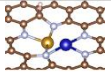
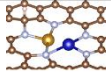
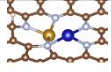
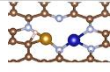
**Supplementary Table 14.** Potential \*H adsorption structures (distance unit: Å) and adsorption free energies on CoCoN<sub>5</sub>-gra.

Co-H	N1-H	N2-H	N3-H	C1-H
				
1.59 / 1.59 -0.22 eV	1.04 0.85 eV	1.05 1.10 eV	1.05 0.94 eV	1.16 -1.38 eV
C2-H	C3-H	C4-H	C5-H	
				
1.12 1.34 eV	1.12 1.13 eV	1.12 1.14 eV	1.12 1.09 eV	

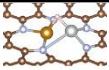
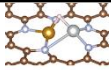
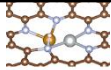
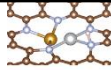
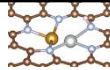
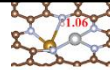
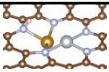
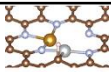
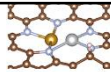
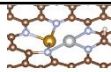
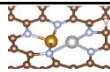
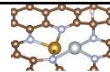
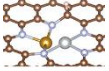
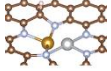
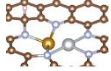
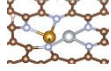
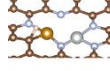
**Supplementary Table 15.** Potential \*H adsorption structures (distance unit: Å) and adsorption free energies on NiNiN<sub>5</sub>-gra.

Ni-H	N1-H	N2-H	N3-H	C1-H
				
1.56 / 1.56 0.29 eV	1.04 0.88 eV	1.04 1.19 eV	1.04 0.91 eV	1.08 -0.64 eV
C2-H	C3-H	C4-H	C5-H	
				
1.12 1.59 eV	1.12 1.16 eV	1.12 1.24 eV	1.12 1.10 eV	

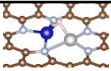
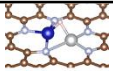
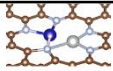
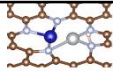
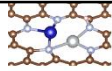
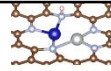
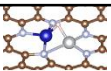
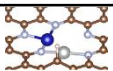
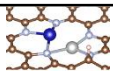
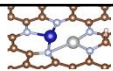
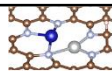
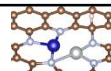
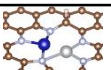
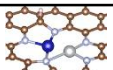
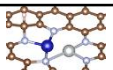
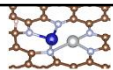
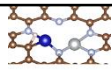
**Supplementary Table 16.** Potential \*H adsorption structures (distance unit: Å) and adsorption free energies on FeCoN<sub>5</sub>-gra.

Fe-H	Co-H	N1-H	N2-H	N3-H	N4-H
 1.79 Å, 1.55 Å -0.18 eV	 1.79 Å, 1.55 Å -0.18 eV	 1.04 Å 0.89 eV	 1.05 Å 1.08 eV	 1.06 Å 1.59 eV	 1.06 Å 1.24 eV
N5-H	C1-H	C2-H	C3-H	C4-H	C5-H
 1.04 Å 1.06 eV	 1.15 Å -1.29 eV	 1.12 Å 1.40 eV	 1.12 Å 1.12 eV	 1.12 Å 1.16 eV	 1.12 Å 1.78 eV
C6-H	C7-H	C8-H	C9-H	C10-H	
 1.12 Å 0.97 eV	 1.12 Å 1.75 eV	 1.12 Å 1.19 eV	 1.12 Å 1.28 eV	 1.14 Å -1.22 eV	

**Supplementary Table 17.** Potential \*H adsorption structures (distance unit: Å) and adsorption free energies on FeNiN<sub>5</sub>-gra.

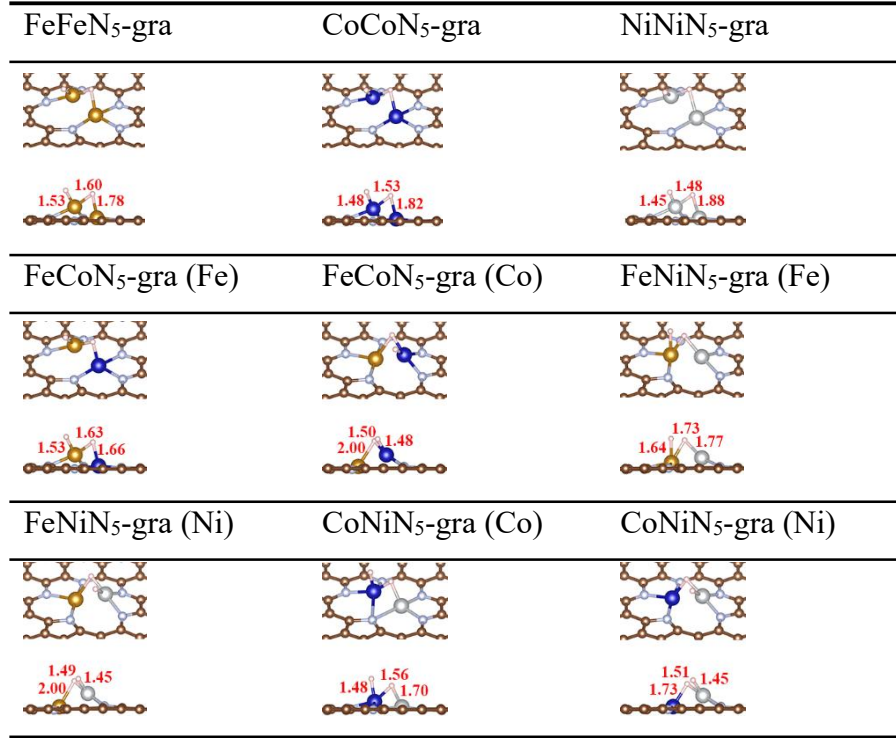
Fe-H	Ni-H	N1-H	N2-H	N3-H	N4-H
 1.75 Å, 1.64 Å -0.04 eV	 1.75 Å, 1.64 Å -0.04 eV	 1.04 Å 0.95 eV	 1.04 Å 1.08 eV	 1.04 Å 0.84 eV	 1.06 Å 0.85 eV
N5-H	C1-H	C2-H	C3-H	C4-H	C5-H
 1.04 Å 1.09 eV	 1.13 Å -1.11 eV	 1.12 Å 2.30 eV	 1.12 Å 1.25 eV	 1.12 Å 2.01 eV	 1.12 Å 1.28 eV
C6-H	C7-H	C8-H	C9-H	C10-H	
 1.12 Å 1.06 eV	 1.12 Å 1.21 eV	 1.12 Å 1.23 eV	 1.12 Å 1.26 eV	 1.15 Å -1.13 eV	

**Supplementary Table 18.** Potential \*H adsorption structures (distance unit: Å) and adsorption free energies on CoNiN<sub>5</sub>-gra. The adsorption on N5 site is unstable and leads to the same structure as metal site.

Co-H	Ni-H	N1-H	N2-H	N3-H	N4-H
 1.54 Å, 1.64 Å -0.06 eV	 1.54 Å, 1.64 Å -0.06 eV	 1.04 Å 0.77 eV	 1.04 Å 1.08 eV	 1.04 Å 0.93 eV	 1.04 Å 1.04 eV
N5-H	C1-H	C2-H	C3-H	C4-H	C5-H
 1.54 Å, 1.64 Å -0.06 eV	 1.13 Å -1.32 eV	 1.12 Å 1.48 eV	 1.12 Å 1.18 eV	 1.12 Å 1.22 eV	 1.12 Å 1.16 eV
C6-H	C7-H	C8-H	C9-H	C10-H	
 1.12 Å 1.00 eV	 1.12 Å 1.11 eV	 1.12 Å 1.15 eV	 1.12 Å 1.35 eV	 1.16 Å -1.40 eV	



**Supplementary Table 19.** Possible HMH structures (distance unit: Å) on MMN<sub>5</sub>-gra/M1M2N<sub>5</sub>-gra.



**Supplementary Table 20** The adsorption free energies (unit: eV) of the first and second H and the distance (unit: Å) between two H atoms in the HMH structures.

Model	$\Delta G^{*H1}$	$\Delta G^{*H2}$	$d_{H-H}$
FeFeN <sub>5</sub> -gra	-0.16	0.19	1.86
CoCoN <sub>5</sub> -gra	-0.22	0.04	1.71
NiNiN <sub>5</sub> -gra	0.29	-0.09	1.66
FeCoN <sub>5</sub> -gra (Fe site)	-0.18	0.25	1.78
FeCoN <sub>5</sub> -gra (Co site)	-0.18	-0.11	1.80
FeNiN <sub>5</sub> -gra (Fe site)	-0.04	0.54	0.99
FeNiN <sub>5</sub> -gra (Ni site)	-0.04	-0.01	1.70
CoNiN <sub>5</sub> -gra (Co site)	-0.06	0.10	1.45
CoNiN <sub>5</sub> -gra (Ni site)	-0.06	0.18	1.71

**Reference:**

[1] Du J, Chen J, Zhang C, Jiang G. Screening out the transition metal single atom supported on onion-like carbon (OLC) for the hydrogen evolution reaction. *Inorg Chem* 2023; 62: 1001-1006. [DOI: 10.1021/acs.inorgchem.2c03922]